



The Leverhulme Trust

# On the strength of being positive

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Jacopo Romoli

Scales, degrees and implicature Workshop, 26.5.2021

## The focus - positive vs negative



- (1) It is **possible** that it contains either a blue ball **or** a yellow ball.

$$\diamond(A \vee B)$$

- (2) It is **certain** that it contains either a blue ball **or** a yellow ball.

$$\square(A \vee B)$$

- (3) It contains either a blue ball **or** a yellow ball.

$$A \vee B$$

## The focus - positive vs negative



- (4) It is **not certain** that it contains both a blue ball **and** a yellow ball.  
 $\neg\Box(A \wedge B)$
- (5) It is **not possible** that it contains both a blue ball **and** a yellow ball.  
 $\neg\Diamond(A \wedge B)$
- (6) It does **not** contain both a blue ball **and** a yellow ball.  
 $\neg(A \wedge B)$

- Large difference in **strength** between positive and negative

- Large difference in **strength** between positive and negative
- **Consequences** for theories of those inferences

- Large difference in **strength** between positive and negative
- **Consequences** for theories of those inferences
- And for accounts of the **differences** between them and regular scalar implicatures

# Background

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The inferences of the positive cases



## The positive cases and their inferences

(7) It is possible that it contains either a blue ball or a yellow ball.

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(7) It is **possible** that it contains either a blue ball **or** a yellow ball.

$\rightsquigarrow$  *it's possible one and possible the other*

$\diamond A \wedge \diamond B$

FREE CHOICE

## The positive cases and their inferences

(7) It is **possible** that it contains either a blue ball **or** a yellow ball.

$\rightsquigarrow$  *it's possible one and possible the other*

$\diamond A \wedge \diamond B$

FREE CHOICE

(8) It is **certain** that it contains either a blue ball **or** a yellow ball.

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(8) It is **certain** that it contains either a blue ball **or** a yellow ball.

$\rightsquigarrow$  *it's not certain one and not certain the other*

$\neg \Box A \wedge \neg \Box B$

DISTRIBUTIVE

## The positive cases and their inferences

(7) It is **possible** that it contains either a blue ball **or** a yellow ball.

$\rightsquigarrow$  *it's possible one and possible the other*

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FREE CHOICE

(8) It is **certain** that it contains either a blue ball **or** a yellow ball.

$\rightsquigarrow$  *it's not certain one and not certain the other*

$\neg \Box A \wedge \neg \Box B$

DISTRIBUTIVE

(9) It contains either a blue ball **or** a yellow ball.

## The positive cases and their inferences

- (7) It is **possible** that it contains either a blue ball **or** a yellow ball.  
 $\rightsquigarrow$  *it's possible one and possible the other*  $\diamond A \wedge \diamond B$   
FREE CHOICE
- (8) It is **certain** that it contains either a blue ball **or** a yellow ball.  
 $\rightsquigarrow$  *it's not certain one and not certain the other*  $\neg \Box A \wedge \neg \Box B$   
DISTRIBUTIVE
- (9) It contains either a blue ball **or** a yellow ball.  
 $\rightsquigarrow$  *the speaker doesn't know which*  $I_s A \wedge I_s B$   
IGNORANCE

# Similarities and differences

- Similarities and differences with regular scalar implicatures

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(10) It is possible that it contains a blue ball.  
 $\rightsquigarrow$  *it's not certain that it does*

$\diamond A$

$\neg \Box A$

SCALAR



# Similarities and differences

- Similarities and differences with regular scalar implicatures

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 $\rightsquigarrow$  *it's not certain that it does*

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SCALAR

- Implicature approach of free choice, distributive, and ignorance inferences

# Similarities and differences

- Similarities and differences with regular scalar implicatures

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SCALAR

- Implicature approach of free choice, distributive, and ignorance inferences
- It accounts for their similarities with regular implicatures

# Similarities and differences

- Similarities and differences with regular scalar implicatures

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 $\rightsquigarrow$  *it's not certain that it does*

$\diamond A$

$\neg \Box A$

SCALAR

- Implicature approach of free choice, distributive, and ignorance inferences
- It accounts for their similarities with regular implicatures
- Supplemented with an account of their differences

# Background

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Starting from free choice

# What is free choice?<sup>1</sup>



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<sup>1</sup>von Wright 1968, Kamp 1974, 1978

## What is free choice?<sup>2</sup>

(11) It is possible that it contains either a blue ball or a yellow ball.

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<sup>2</sup>von Wright 1968, Kamp 1974, 1978

## What is free choice?<sup>2</sup>

- (11) It is possible that it contains either a blue ball or a yellow ball.  
↪ *It is possible that it contains one and possible it contains the other*

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<sup>2</sup>von Wright 1968, Kamp 1974, 1978

# Why problematic?

- It doesn't follow from the [standard meanings](#) of modals and disjunction



To illustrate

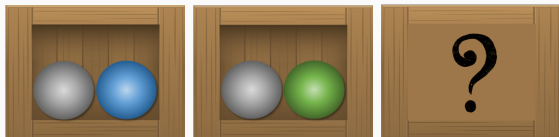


## To illustrate



- We don't know what is in the mystery box, but we know it is **identical** to one of the overt boxes

To illustrate



## Why problematic: the meaning of modals

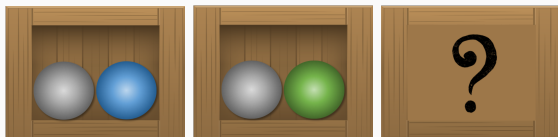
(12) It is possible that it contains a blue ball

◇A

## Why problematic: the meaning of modals

(12) It is **possible** that it contains a blue ball

◇A



## Why problematic: the meaning of disjunction

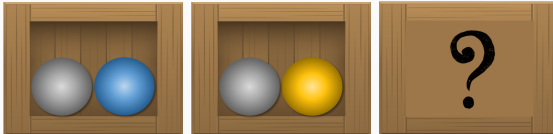
(13) It contains a blue or a yellow ball

$(A \vee B)$

# Why problematic: the meaning of disjunction

(13) It contains a blue or a yellow ball

$(A \vee B)$



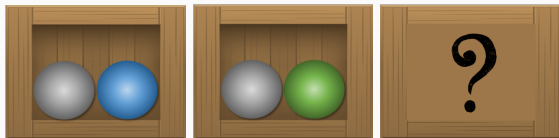
## Why problematic

(14) It is possible that it contains either a blue or a yellow ball  $\diamond(A \vee B)$



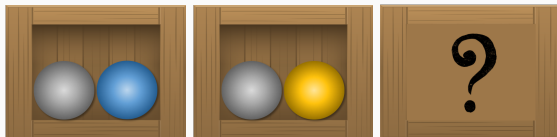
# Why problematic

(14) It is **possible** that it contains either a blue **or** a yellow ball  $\diamond(A \vee B)$



# Why problematic

(15) It is **possible** that it contains either a blue **or** a yellow ball  $\diamond(A \vee B)$



# The general question

- Where does free choice come from?

# Background

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The implicature approach

# The implicature approach<sup>3</sup>

- The meaning of **disjunction** and **modals** are standard

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<sup>3</sup>Fox 2007, Klinedinst 2006, Chierchia 2013, Chemla 2010, Franke 2013, Santorio & Romoli 2018, Bar-Lev & Fox 2017 a.o

# The implicature approach<sup>3</sup>

- The meaning of **disjunction** and **modals** are standard
- Free choice is an **implicature**

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<sup>3</sup>Fox 2007, Klinedinst 2006, Chierchia 2013, Chemla 2010, Franke 2013, Santorio & Romoli 2018, Bar-Lev & Fox 2017 a.o

(16) It is possible A or B =  $\diamond A \vee \diamond B$

## Free choice and the implicature approach

(16) It is possible A or B =  $\diamond A \vee \diamond B$

(17)  $\left\{ \begin{array}{l} \text{It is possible A} \quad \diamond A \\ \text{It is possible B} \quad \diamond B \\ \dots \end{array} \right\}$



(18)  $\left\{ \begin{array}{l} \text{It is possible A } \diamond A \\ \text{It is possible B } \diamond B \end{array} \right\}$

(18)  $\left\{ \begin{array}{l} \text{It is possible A } \diamond A \\ \text{It is possible B } \diamond B \end{array} \right\}$

(19)  $\text{IMP}[\text{It is possible A or B}] \rightsquigarrow$

## Free choice and the implicature approach

$$(18) \quad \left\{ \begin{array}{l} \text{It is possible A} \quad \diamond A \\ \text{It is possible B} \quad \diamond B \end{array} \right\}$$

$$(19) \quad \text{IMP}[\text{It is possible A or B}] \rightsquigarrow \text{It is possible A and It is possible B} \quad \diamond A \wedge \diamond B$$

# Background

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Related inferences

(20) It is **certain** that it contains either a blue ball **or** a yellow ball.

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<sup>4</sup>Sauerland 2004, Chierchia et al 2012, Crnic et al 2015, Santorio and Romoli 2018

- (20) It is **certain** that it contains either a blue ball **or** a yellow ball.  
↪ *It is not certain one and not certain the other*

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<sup>4</sup>Sauerland 2004, Chierchia et al 2012, Crnic et al 2015, Santorio and Romoli 2018

## Distributivity and the implicature approach

(21) It is certain A or B =  $\Box(A \vee B)$

# Distributivity and the implicature approach

(21) It is certain A or B =  $\Box(A \vee B)$

(22)  $\left\{ \begin{array}{ll} \text{It is certain A} & \Box A \\ \text{It is certain B} & \Box B \\ \dots & \end{array} \right\}$



## Distributivity and the implicature approach

(23)  $\left\{ \begin{array}{l} \text{It is certain A} \quad \Box A \\ \text{It is certain B} \quad \Box B \end{array} \right\}$

(24)  $\text{IMP}[\text{It is certain A or B}] \rightsquigarrow$

## Distributivity and the implicature approach

$$(23) \quad \left\{ \begin{array}{l} \text{It is certain A} \quad \Box A \\ \text{It is certain B} \quad \Box B \end{array} \right\}$$

$$(24) \quad \text{IMP}[\text{It is certain A or B}] \rightsquigarrow \text{It is not certain A and It is not certain B} \quad \neg\Box A \wedge \neg\Box B$$

# Ignorance and the implicature approach<sup>5</sup>

(25) It contains either a blue ball or a yellow ball.

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<sup>5</sup>Gazdar 1979, Sauerland 2004, Fox 2007, Meyer 2013, Buccola and Haida 2019

- (25) It contains either a blue ball or a yellow ball.  
↪ *The speaker doesn't know which one*

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<sup>5</sup>Gazdar 1979, Sauerland 2004, Fox 2007, Meyer 2013, Buccola and Haida 2019

# Ignorance and the implicature approach<sup>6</sup>

(26) A or B =  $A \vee B$

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<sup>6</sup>Gazdar 1979, Sauerland 2004, Fox 2007, Meyer 2013, Buccola and Haida 2019

# Ignorance and the implicature approach<sup>7</sup>

(27) A or B

{ A, B,  $\neg$ A,  $\neg$ B }

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<sup>7</sup>Gazdar 1979, Sauerland 2004, Fox 2007, Meyer 2013, Buccola and Haida 2019

# Ignorance and the implicature approach<sup>7</sup>

(27) A or B  $\{ A, B, \neg A, \neg B \}$

(28) **IMP**[K[A or B]]  $\{ K[A], K[B] \}$

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<sup>7</sup>Gazdar 1979, Sauerland 2004, Fox 2007, Meyer 2013, Buccola and Haida 2019

# Ignorance and the implicature approach<sup>7</sup>

(27) A or B  $\{ A, B, \neg A, \neg B \}$

(28) **IMP**[K[A or B]]  $\{ K[A], K[B] \}$

$\rightsquigarrow$  *the speaker doesn't know whether A **and** doesn't know whether B*

$I_s A \wedge I_s B$

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<sup>7</sup>Gazdar 1979, Sauerland 2004, Fox 2007, Meyer 2013, Buccola and Haida 2019



## Free choice, the others, and implicatures<sup>8</sup>

- The [implicature approach](#) to free choice, distributive inferences, and ignorance has been prominent

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<sup>8</sup>Fox 2007; see also Franke 2011, Geurts 2010, Schwarz 2020 and Katzir and Fox 2019

## Free choice, the others, and implicatures<sup>8</sup>

- The **implicature approach** to free choice, distributive inferences, and ignorance has been prominent
- Free choice as a **testing ground** for theories of implicatures

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<sup>8</sup>Fox 2007; see also Franke 2011, Geurts 2010, Schwarz 2020 and Katzir and Fox 2019

# Background

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**Free choice, distributivity, ignorance,  
and scalar diversity**

- Large **differences** among different scalar inferences

- Large **differences** among different scalar inferences
  - Comprehension

- Large **differences** among different scalar inferences
  - Comprehension
  - Processing

- Large **differences** among different scalar inferences
  - Comprehension
  - Processing
  - Acquisition

## Free choice and scalar diversity<sup>9</sup>

- Free choice appears more robust than scalar implicatures

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<sup>9</sup>Chemla 2009, Chemla and Bott 2013, Tieu et al 2016, Meyer and Feiman 2020



## Free choice and scalar diversity<sup>9</sup>

- Free choice appears more robust than scalar implicatures
- It differs in its processing profile from scalar implicatures

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<sup>9</sup>Chemla 2009, Chemla and Bott 2013, Tieu et al 2016, Meyer and Feiman 2020

## Free choice and scalar diversity<sup>9</sup>

- Free choice appears more robust than scalar implicatures
- It differs in its processing profile from scalar implicatures
- It is also acquired earlier

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<sup>9</sup>Chemla 2009, Chemla and Bott 2013, Tieu et al 2016, Meyer and Feiman 2020

- Distributive and ignorance inferences investigated less

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<sup>10</sup>Van Tiel and Schaeken 2017, Pagliarini et al 2018, Hochstein et al 2016

- Distributive and ignorance inferences investigated less
- Similar differences to regular implicatures

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<sup>10</sup>Van Tiel and Schaeken 2017, Pagliarini et al 2018, Hochstein et al 2016

- Free choice and related inferences appear more **robust**, **faster** to process and **easier** to acquire than regular scalar implicatures

- Free choice and related inferences appear more **robust**, **faster** to process and **easier** to acquire than regular scalar implicatures
- **Challenging** for the implicature approach

# Background

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**Alternatives as the source of scalar  
diversity**

# Alternatives and scalar diversity

- The **source** of these differences would be in alternatives



## The source would be alternatives

(29) It possible that it contains a blue ball

- (29) It **possible** that it contains a blue ball  
     $\rightsquigarrow$  *it is not certain that it contains a blue ball*

## The source would be alternatives

(29) It **possible** that it contains a blue ball  
 $\rightsquigarrow$  *it is not certain that it contains a blue ball*

(30) { It is **certain** that it contains a blue ball }

## The source would be alternatives

(31) It is possible that it contains a blue ball or a yellow ball

- (31) It is possible that it contains a blue ball or a yellow ball  
↪ *it is possible one and it is possible the other*

## The source would be alternatives

(31) It is possible that it contains a blue ball or a yellow ball  
 $\rightsquigarrow$  *it is possible one and it is possible the other*

(32)  $\left\{ \begin{array}{l} \text{It is possible that it contains a blue ball,} \\ \text{It is possible that it contains a yellow ball} \end{array} \right\}$

## The source would be alternatives

(33) It is possible that it contains a blue ball or a yellow ball.

*↪ it is possible one and it is possible the other*

(34)  $\left\{ \begin{array}{l} \text{It is possible that it contains a blue ball,} \\ \text{it is possible that it contains a yellow ball} \end{array} \right\}$

## The source would be alternatives

(35) It is possible that it contains a blue ball or a yellow ball

$\rightsquigarrow$  *it is possible one and it is possible the other*

(36)  $\left\{ \begin{array}{l} \text{It is possible that it contains a blue ball,} \\ \text{It is possible that it contains a yellow ball} \end{array} \right\}$



## The source would be alternatives

(37) It is certain that it contains a blue ball or a yellow ball  
 $\rightsquigarrow$  *it is not certain one and it is not certain the other*

(38)  $\left\{ \begin{array}{l} \text{It is certain that it contains a blue ball,} \\ \text{It is certain that it contains a yellow ball} \end{array} \right\}$

## The source would be alternatives

(39) It contains a blue ball or a yellow ball  
↪ *the speaker doesn't know which*

(40) { It contains a blue ball,  
It contains a yellow ball }  
{ ... }

# The hypothesis about alternatives<sup>11</sup>

- Alternatives that **do not involve** lexical substitution are more robust, faster to process, and easier to acquire

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<sup>11</sup>Chemla and Bott 2014, Tieu et al 2016, Barner et al 2013, Singh et al 2016; for variants of it see Bar-Lev and Fox 2020 and Singh 2019

# The project

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# **The project**

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**Testing the hypothesis further**

- Testing the [hypothesis](#) about alternatives further

- Testing the **hypothesis** about alternatives further
- Looking at other constructions with related **inferences**

- Testing the **hypothesis** about alternatives further
- Looking at other constructions with related **inferences**
- Involving **the same type** of alternatives as the inferences above



- Their inferences should pattern with those above and unlike regular implicatures

## The positive cases again

- (41) It is possible that it contains either a blue ball or a yellow ball.  
↔ *it's possible one and possible the other*

## The positive cases again

- (41) It is **possible** that it contains either a blue ball **or** a yellow ball.  
↪ *it's possible one and possible the other*
- (42) It is **certain** that it contains either a blue ball **or** a yellow ball.  
↪ *it's not certain one and not certain the other*

## The positive cases again

- (41) It is **possible** that it contains either a blue ball **or** a yellow ball.  
↪ *it's possible one and possible the other*
- (42) It is **certain** that it contains either a blue ball **or** a yellow ball.  
↪ *it's not certain one and not certain the other*
- (43) It contains either a blue ball **or** a yellow ball.  
↪ *the speaker doesn't know which*

## The negative counterparts

- (44) It is not **certain** that it contains both a blue ball **and** a yellow ball.  
↔ *it's not certain one and not certain the other*

## The negative counterparts

- (44) It is not **certain** that it contains both a blue ball **and** a yellow ball.  
↪ *it's not certain one and not certain the other*
- (45) It is not **possible** that it contains both a blue ball **and** a yellow ball.  
↪ *it's possible one and possible the other*

## The negative counterparts

- (44) It is not **certain** that it contains both a blue ball **and** a yellow ball.  
↪ *it's not certain one and not certain the other*
- (45) It is not **possible** that it contains both a blue ball **and** a yellow ball.  
↪ *it's possible one and possible the other*
- (46) It doesn't contain both a blue ball **and** a yellow ball.  
↪ *the speaker doesn't know which*

# **The project**

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**The implicature approach**



(47) It is not certain that A and B =  $\neg\Box A \vee \neg\Box B$

## Negative free choice

(47) It is not certain that A and B =  $\neg\Box A \vee \neg\Box B$

(48)  $\left\{ \begin{array}{l} \text{It is not certain that A} \quad \neg\Box A \\ \text{It is not certain that B} \quad \neg\Box B \end{array} \right\}$

$$(49) \quad \left\{ \begin{array}{l} \text{It is not certain that A} \quad \neg\Box A \\ \text{It is not certain that B} \quad \neg\Box B \end{array} \right\}$$

$$(49) \quad \left\{ \begin{array}{l} \text{It is not certain that A} \quad \neg\Box A \\ \text{It is not certain that B} \quad \neg\Box B \end{array} \right\}$$

$$(50) \quad \text{IMP[ It is not certain A and B] } \rightsquigarrow \text{It is not certain A and It is not certain B} \quad \neg\Box A \wedge \neg\Box B$$

(51) It is not possible that A and B =  $\neg\Diamond(A \wedge B)$

## Negative distributivity

(51) It is not possible that A and B =  $\neg\Diamond(A \wedge B)$

(52)  $\left\{ \begin{array}{l} \text{It is not possible that A} \quad \neg\Diamond A \\ \text{It is not possible that B} \quad \neg\Diamond B \end{array} \right\}$

## Negative distributivity

$$(53) \quad \left\{ \begin{array}{l} \text{It is not possible that A} \quad \neg\Diamond A \\ \text{It is not possible that B} \quad \neg\Diamond B \end{array} \right\}$$

$$(54) \quad \text{IMP[ It is not possible A and B] } \rightsquigarrow \\ \text{It is possible A and it is possible B}$$

$$\Diamond A \wedge \Diamond B$$

# Negative ignorance

(55) not both A and B =  $\neg(A \wedge B)$



## Negative ignorance

$$(56) \quad \{ \neg A, \neg B, A, B \} \qquad \{ K[\neg A], K[\neg B] \}$$

$$(57) \quad \text{not both } A \text{ and } B \qquad \text{IMP}[K[\text{not both } A \text{ and } B]]$$

$\rightsquigarrow$  *The speaker doesn't know whether A **and** doesn't know whether B*  $I_s A \wedge I_s B$

# The prediction

- The implicature approach predicts the **negative inferences** in the same way

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- The implicature approach predicts the **negative inferences** in the same way
- On the basis of the **same type of alternatives**

# The prediction

- The implicature approach predicts the **negative inferences** in the same way
- On the basis of the **same type of alternatives**
- Their inferences should **pattern with** their positive counterparts and unlike regular implicatures

- Do the **negative inferences** behave similarly to their **positive counterparts** and unlike regular scalar implicatures?

# Collaborators



Alternatives in the foundations of implicit meanings



# The rest of today

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1. The experiment



# The rest of today

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1. The experiment
2. The challenge

# The rest of today

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1. The experiment
2. The challenge
3. Conclusion and looking ahead

## **The previous study**

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## Negative Free Choice\*

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**Abstract** FREE CHOICE (FC) is an inference arising from the interaction between existential modals and disjunction. For instance, a sentence of the form *permitted(A or B)* gives rise to the inference  $\Diamond A \wedge \Diamond B$ . Many competing theories of FC have

- Comparing positive vs negative free choice with deontic modals against each other

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<sup>12</sup>Building on Chemla 2009 and Marty et al 2015 and Tieu et al 2018

# What we did<sup>12</sup>

- Comparing positive vs negative free choice with deontic modals against each other
- And to the corresponding cases with regular scalar implicatures

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<sup>12</sup>Building on Chemla 2009 and Marty et al 2015 and Tieu et al 2018

- Negative Free Choice much weaker than its positive counterpart

# The main results

- Negative Free Choice much weaker than its positive counterpart
- No corresponding difference between positive and negative regular scalar implicatures



# The experiment

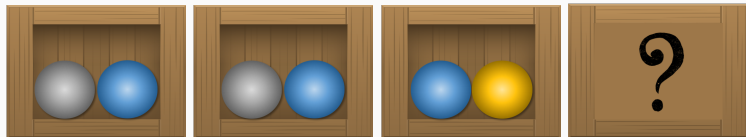
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# The goal

- Comparing positive and negative inferences, free choice, distributive, and ignorance

# The goal

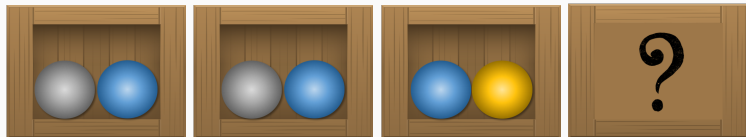
- Comparing positive and negative inferences, free choice, distributive, and ignorance
- Comparing them to positive and negative regular implicatures



- **Mystery box paradigm:** identical to one of the overt boxes

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<sup>13</sup>adapted from Noveck 2001; see also Moscati et al 2015

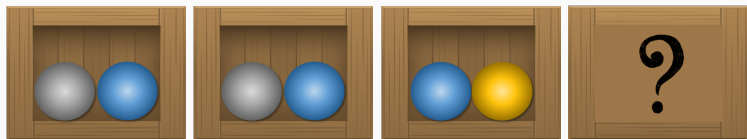


- **Mystery box paradigm**: identical to one of the overt boxes
- Task: whether the sentence was a **good description** of the picture

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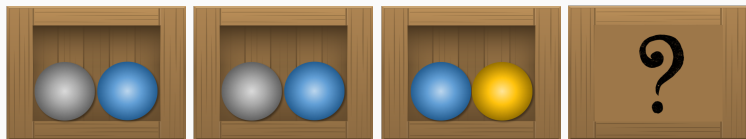
<sup>13</sup>adapted from Noveck 2001; see also Moscati et al 2015

## Training with feedback



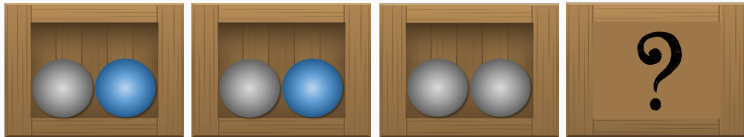
(58) It is certain that the mystery box contains a blue ball

## Training with feedback



(59) It is not possible that the mystery box contains a yellow ball

## Material: FC targets



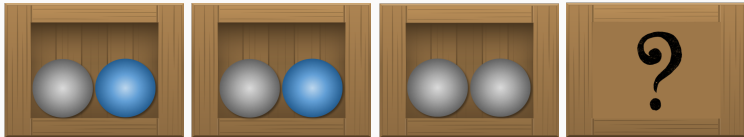
- (60) It is possible that the mystery box contains either a blue ball or a yellow ball

$\diamond A \vee \diamond B$

LITERAL MEANING



## Material: FC targets



- (60) It is possible that the mystery box contains either a blue ball or a yellow ball

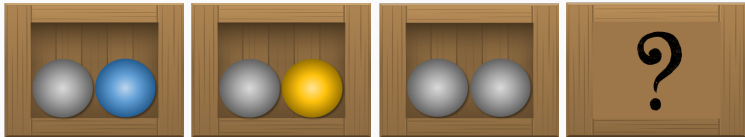
$\diamond A \vee \diamond B$

$\diamond A \wedge \diamond B$

LITERAL MEANING

FREE CHOICE MEANING

## Material: FC true control



- (61) It is possible that the mystery box contains either a blue ball or a yellow ball

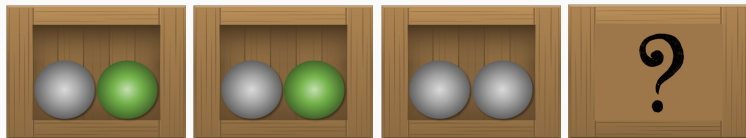
$\diamond A \vee \diamond B$

$\diamond A \wedge \diamond B$

LITERAL MEANING

FREE CHOICE MEANING

## Material: FC false control



- (62) It is possible that the mystery box contains either a blue ball or a yellow ball

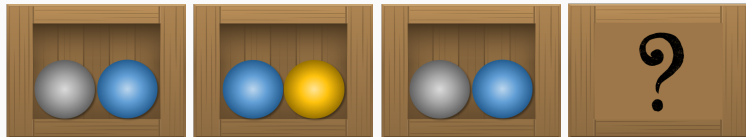
$\diamond A \vee \diamond B$

$\diamond A \wedge \diamond B$

LITERAL MEANING

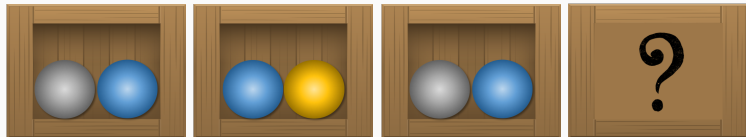
FREE CHOICE MEANING

## Material: NFC targets



- (63) It is not certain that the mystery box contains both a blue ball and a yellow ball

## Material: NFC targets

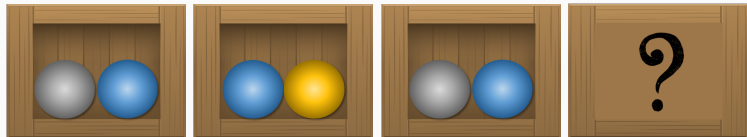


- (63) It is not certain that the mystery box contains both a blue ball and a yellow ball

$\neg \Box A \vee \neg \Box B$

LITERAL MEANING

## Material: NFC targets



- (63) It is not certain that the mystery box contains both a blue ball and a yellow ball

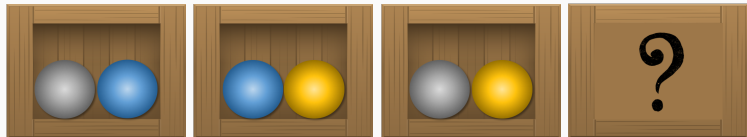
$\neg \Box A \vee \neg \Box B$

$\neg \Box A \wedge \neg \Box B$

LITERAL MEANING

NEGATIVE FREE CHOICE MEANING

## Material: NFC true control



- (64) It is not certain that the mystery box contains both a blue ball and a yellow ball

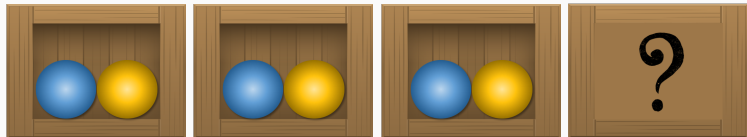
$\neg \Box A \vee \neg \Box B$

$\neg \Box A \wedge \neg \Box B$

LITERAL MEANING

NEGATIVE FREE CHOICE MEANING

## Material: NFC false control



- (65) It is not certain that the mystery box contains both a blue ball and a yellow ball

$\neg \Box A \vee \neg \Box B$

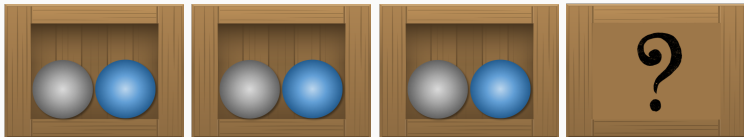
$\neg \Box A \wedge \neg \Box B$

LITERAL MEANING

NEGATIVE FREE CHOICE MEANING

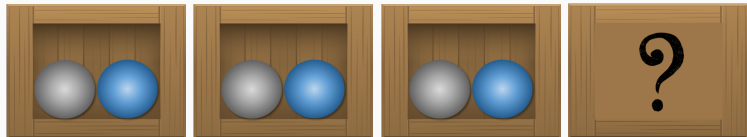


## Material: Dist targets



- (66) It is certain that the mystery box contains either a blue ball or a yellow ball

## Material: Dist targets

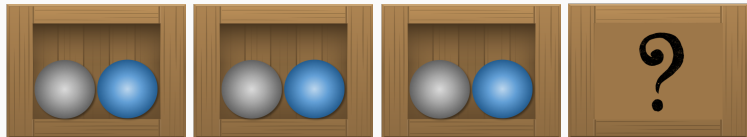


- (66) It is certain that the mystery box contains either a blue ball or a yellow ball

$\square(A \vee B)$

LITERAL MEANING

## Material: Dist targets



- (66) It is certain that the mystery box contains either a blue ball or a yellow ball

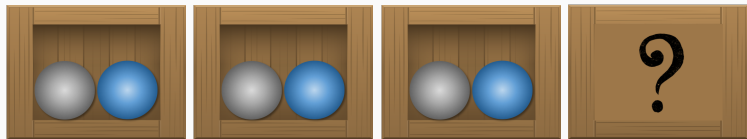
$\Box(A \vee B)$

$\neg\Box A \wedge \neg\Box B$

LITERAL MEANING

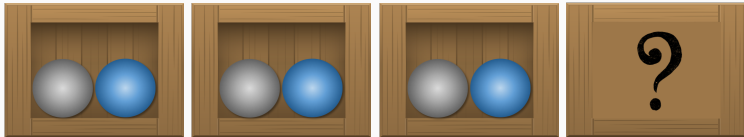
DISTRIBUTIVE MEANING

## Material: NDist targets



- (67) It is not possible that the mystery box contains both a blue ball and a yellow ball

## Material: NDist targets

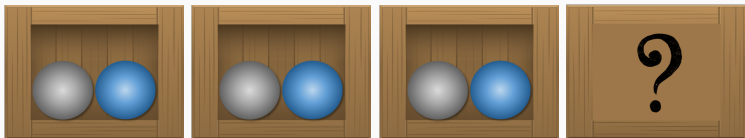


- (67) It is not possible that the mystery box contains both a blue ball and a yellow ball

$\neg\Diamond(A \wedge B)$

LITERAL MEANING

## Material: NDist targets



- (67) It is not possible that the mystery box contains both a blue ball and a yellow ball

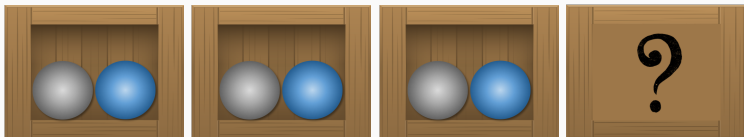
$\neg\Diamond(A \wedge B)$

$\Diamond A \wedge \Diamond B$

LITERAL MEANING

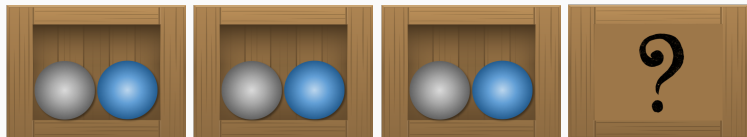
DISTRIBUTIVE MEANING

## Material: II targets



(68) The mystery box contains either a blue ball or a yellow ball

## Material: $\perp$ targets



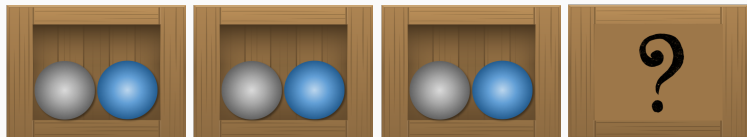
(68) The mystery box contains either a blue ball or a yellow ball

$A \vee B$

LITERAL MEANING



## Material: $\perp$ targets



(68) The mystery box contains either a blue ball or a yellow ball

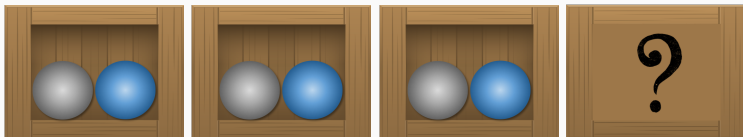
$A \vee B$

$\neg I_S A \wedge \neg I_S B$

LITERAL MEANING

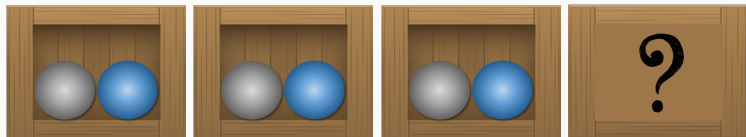
IGNORANCE INFERENCE

## Material: NII targets



(69) The mystery box doesn't contain both a blue ball and a yellow ball

## Material: NII targets

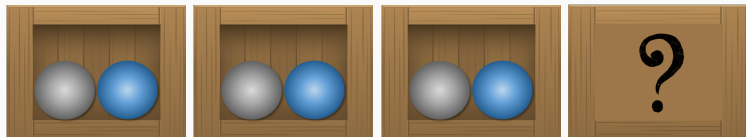


(69) The mystery box doesn't contain both a blue ball and a yellow ball

$\neg(A \wedge B)$

LITERAL MEANING

## Material: NII targets



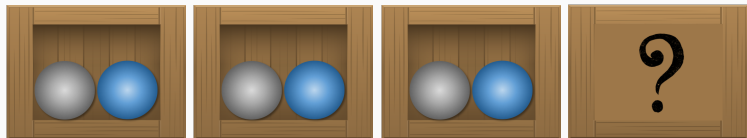
(69) The mystery box doesn't contain both a blue ball and a yellow ball

$\neg(A \wedge B)$

$\neg I_S A \wedge \neg I_S B$

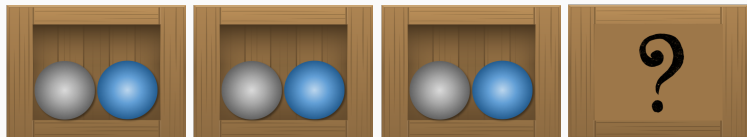
LITERAL MEANING  
IGNORANCE INFERENCE

## Material: SI targets



(70) It is possible that the mystery box contains a blue ball

## Material: SI targets

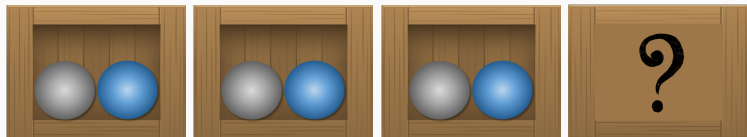


(70) It is possible that the mystery box contains a blue ball

$\diamond A \vee \square A$

LITERAL MEANING

## Material: SI targets



(70) It is possible that the mystery box contains a blue ball

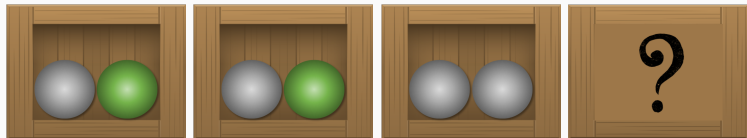
$\diamond A \vee \square A$

$\diamond A \wedge \neg \square A$

LITERAL MEANING

SI MEANING

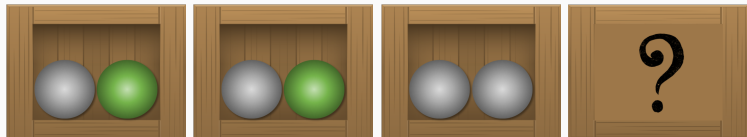
## Material: ISI targets



(71) It is not certain that the mystery box contains a blue ball



## Material: ISI targets

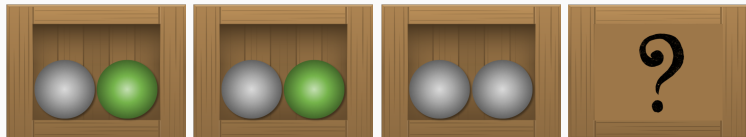


(71) It is not certain that the mystery box contains a blue ball

$\neg \Diamond A \vee \neg \Box A$

LITERAL MEANING

## Material: ISI targets



(71) It is not certain that the mystery box contains a blue ball

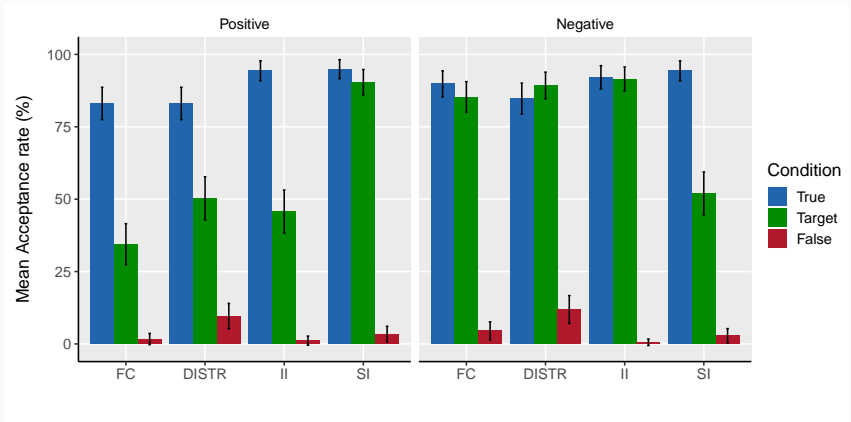
$\neg \diamond A \vee \neg \square A$

$\diamond A \wedge \neg \square A$

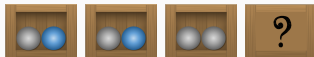
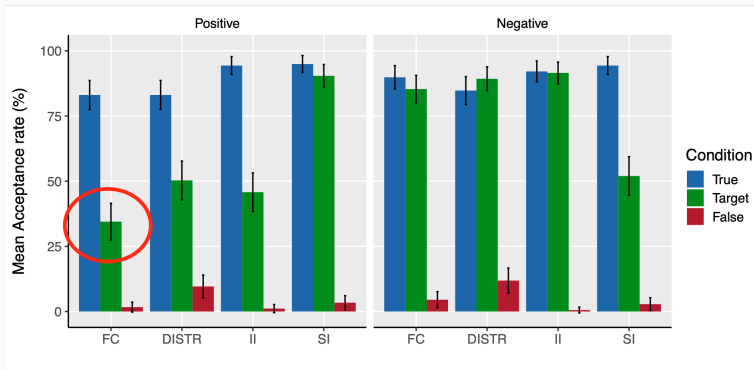
LITERAL MEANING

SI MEANING

# Results

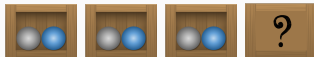
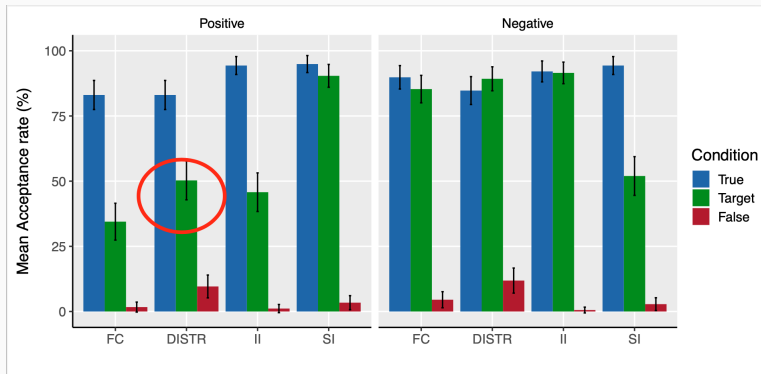


# Results



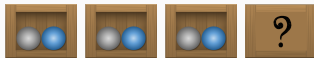
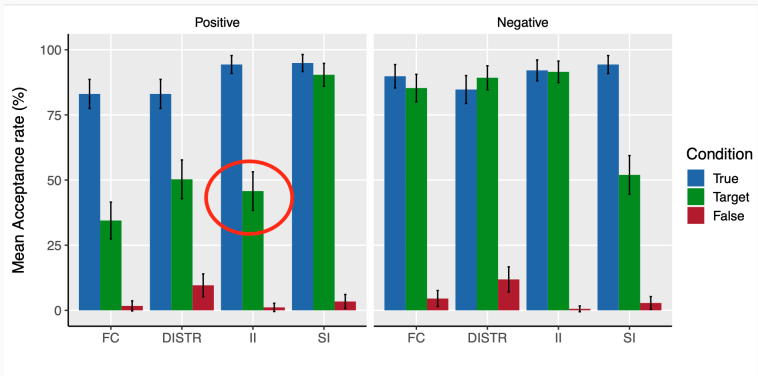
It is possible that it contains either A or B

# Results



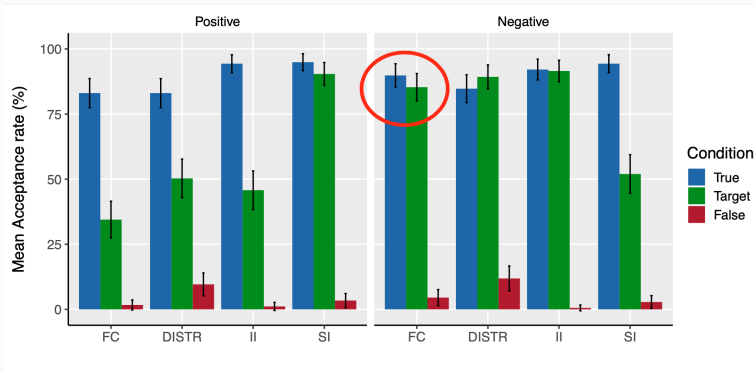
It is certain that it contains either A or B

# Results



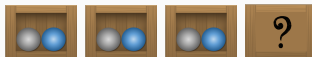
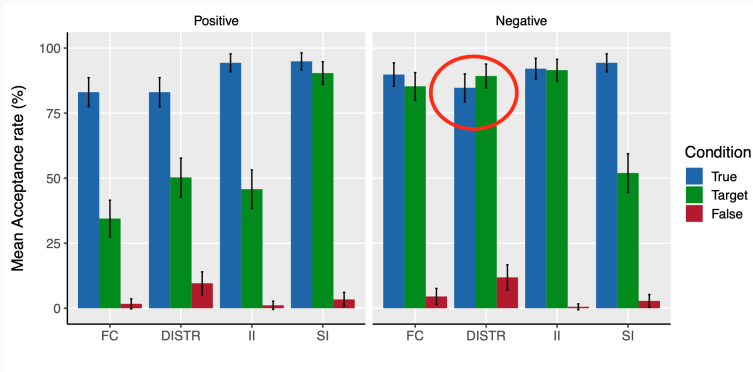
It contains either A or B

# Results



It is not certain that it contains both A and B

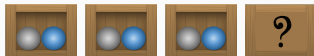
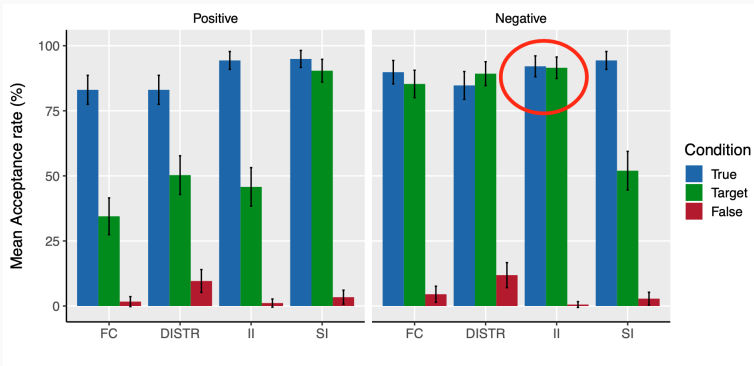
# Results



It is not possible that it contains both A and B

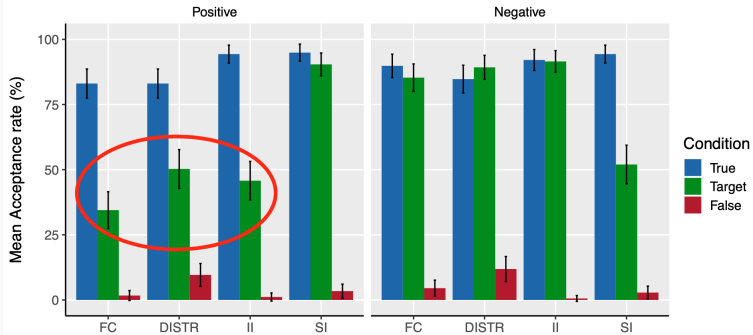


# Results

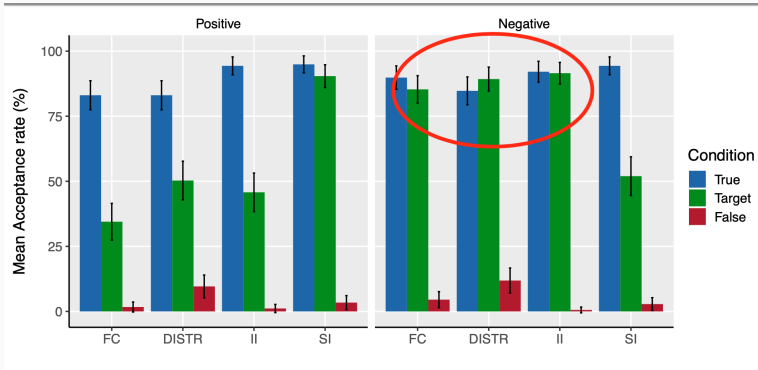


It doesn't contain both A and B

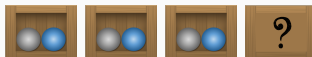
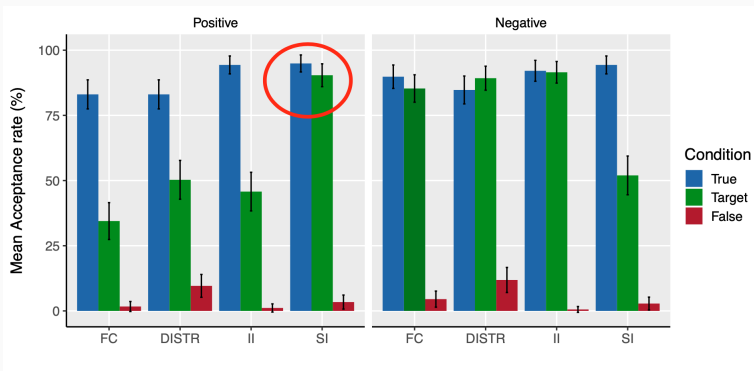
# Results



# Results

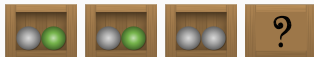
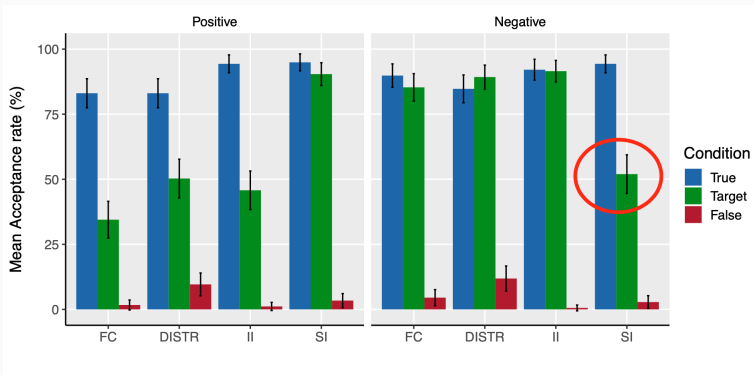


# Results



It is possible that A

# Results



It is not certain that A

## **General Discussion and conclusion**

---

# The main results

- Our results are **challenging** the hypothesis about alternatives and the implicature approach

# The hypothesis again

- Alternatives that do not involve lexical substitution are **more robust**, faster to process, and easier to acquire



- The positive and negative versions are all based on alternatives that do not involve lexical substitutions

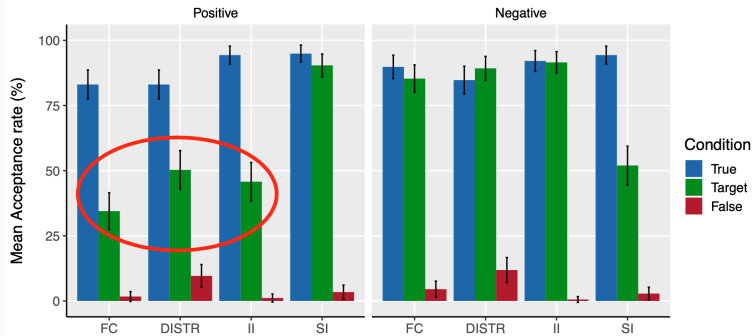
# Why challenging

- The positive and negative versions are all based on alternatives that do not involve lexical substitutions
- Why so much difference in the rates of endorsement?

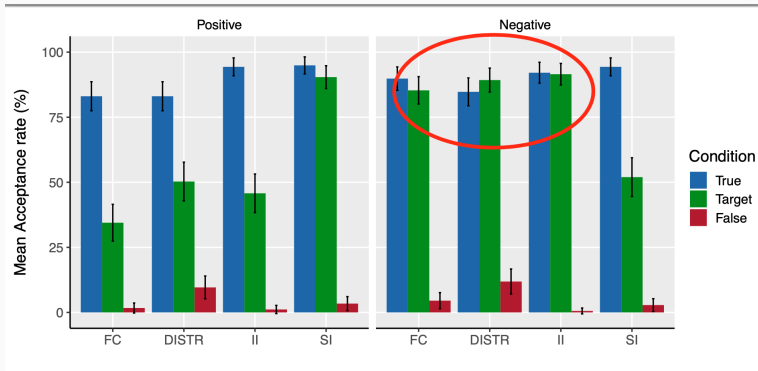
# Why challenging

- The positive and negative versions are all based on alternatives that do not involve lexical substitutions
- Why so much difference in the rates of endorsement?
- With no corresponding difference between regular SIs and ISIs

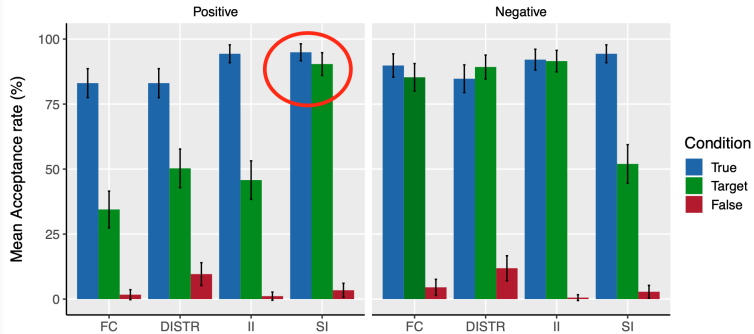
# Back to the results



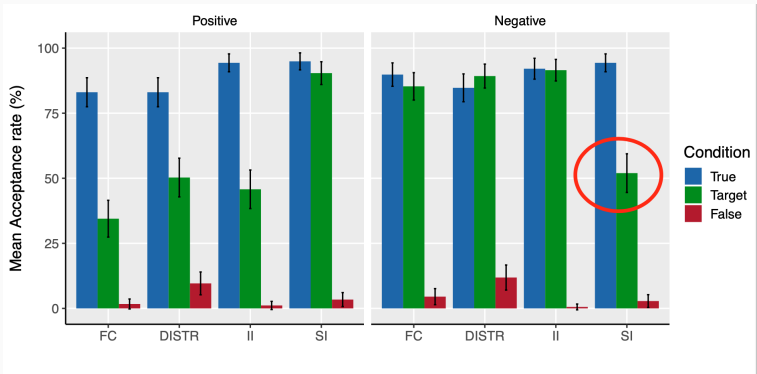
# Back to the results



# Back to the results



# Back to the results



# What we need

- An account of [the difference](#) between positive and negative



# What we need

- An account of **the difference** between positive and negative
- not extending to regular implicatures

# Three directions

- A hybrid approach

# Three directions

- A hybrid approach
- More alternatives

# Three directions

- A hybrid approach
- More alternatives
- A relevance-based account

- Negative vs positive as a powerful perspective

- Negative vs positive as a **powerful perspective**
- To learn more about those inferences and the **alternatives** they arise from

# Conclusion

- Negative vs positive as a **powerful perspective**
- To learn more about those inferences and the **alternatives** they arise from
- And hypotheses about the **differences** among them

Thanks!

Thanks!



**What then**

---

**What then**

---

**Giving up a unified account**

# A hybrid account

- Non-impicature approach to FC<sup>14</sup>

---

<sup>14</sup>Not extending to NFC though e.g. Goldstein 2019 but not Aloni 2018 or Willer 2018

# A hybrid account

- Non-implicature approach to FC<sup>14</sup>
- Implicature approach to NFC

---

<sup>14</sup>Not extending to NFC though e.g. Goldstein 2019 but not Aloni 2018 or Willer 2018

**What then**

---

**More alternatives**

- NFC is weaker because it involves more alternatives

---

<sup>15</sup>Bar-lev and Fox 2017 2020

## More alternatives to consider<sup>15</sup>

- NFC is weaker because it involves more alternatives
- When those additional alternatives are factored in no inference arises

---

<sup>15</sup>Bar-lev and Fox 2017 2020

- The gist of the idea is that negation can be replaced by  $\text{EXH}$



## Back to negative free choice

$$(72) \quad \left\{ \begin{array}{l} \text{It is not required that A} \quad \neg\Box A \\ \text{It is not required that B} \quad \neg\Box B \end{array} \right\}$$

$$(73) \quad \text{EXH[ It is not required A and B] = } \quad \neg\Box A \wedge \neg\Box B$$

*It is not required A and It is not required B*

## Back to negative free choice

$$(74) \left\{ \begin{array}{ll} \text{not[It is required that A and B]} & \neg\Box(A \wedge B) \\ \text{not[It is required that A]} & \neg\Box A \\ \text{not[It is required that B]} & \neg\Box B \\ \text{not[It is required that A or B]} & \neg\Box(A \vee B) \\ \text{EXH[It is required that A and B]} & \Box(A \wedge B) \\ \text{EXH[It is required that A]} & \Box A \wedge \neg\Box B \\ \text{EXH[It is required that B]} & \Box B \wedge \neg\Box A \\ \text{EXH[It is required that A or B]} & \Box(A \vee B) \wedge \neg\Box(A \wedge B) \end{array} \right\}$$

## Back to negative free choice

$$(74) \left\{ \begin{array}{ll} \text{not[It is required that A and B]} & \neg\Box(A \wedge B) \\ \text{not[It is required that A]} & \neg\Box A \\ \text{not[It is required that B]} & \neg\Box B \\ \text{not[It is required that A or B]} & \neg\Box(A \vee B) \\ \text{EXH[It is required that A and B]} & \Box(A \wedge B) \\ \text{EXH[It is required that A]} & \Box A \wedge \neg\Box B \\ \text{EXH[It is required that B]} & \Box B \wedge \neg\Box A \\ \text{EXH[It is required that A or B]} & \Box(A \vee B) \wedge \neg\Box(A \wedge B) \end{array} \right\}$$

$$(75) \quad \text{EXH[ It is not required A and B]} = \text{It is not required A or It is not required B} \quad \neg\Box A \vee \neg\Box B$$

# The problem

(76) EXH[ It is not required that A] =  
It is not required that A but it is permitted that A ISI

# The problem

(76) EXH[ It is not required that A ] =  
It is not required that A but it is permitted that A ISI

(77)  $\left\{ \begin{array}{ll} \text{It is not required that A} & \neg\Box A \\ \text{It is not permitted that A} & \neg\Diamond A \end{array} \right\}$

# The problem

$$(78) \quad \left\{ \begin{array}{ll} \text{not[It is required that A]} & \neg\Box A \\ \text{not[It is permitted that A]} & \neg\Diamond A \\ \text{EXH[It is required that A]} & \Box A \\ \text{EXH[It is permitted that A]} & \Diamond A \wedge \neg\Box A \end{array} \right\}$$

# The problem

$$(78) \left\{ \begin{array}{ll} \text{not[It is required that A]} & \neg\Box A \\ \text{not[It is permitted that A]} & \neg\Diamond A \\ \text{EXH[It is required that A]} & \Box A \\ \text{EXH[It is permitted that A]} & \Diamond A \wedge \neg\Box A \end{array} \right\}$$

$$(79) \text{EXH[ It is not required that A]} = \\ \text{It is not required that A}$$

NO ISI

- The idea allows to account for the difference between FC and NFC



- The idea allows to account for the difference between FC and NFC
- It incorrectly extends to predict that ISIs should be weaker than SIs

**What then**

---

**Relevance**

- The implicature approach to free choice

- The implicature approach to free choice
- A notion of Relevance and the pragmatics of negation

- A sentence is relevant if its meaning addresses the understood QUD

- Implicatures only arise from relevant alternatives

## Relevance

A proposition  $p$  is relevant in a context  $c$  and the partition  $Q$  of the context set  $c$  induced by the current QUD of  $c$  if it is contextually equivalent to a cell or union of cells of  $Q$

---

<sup>16</sup>Heim 2011, Spector 2010

# The pragmatics of negation

- A negative sentence is associated with the expectation that its prejacent is/was possible



# The pragmatics of negation

- A negative sentence is associated with the expectation that its prejacent is/was possible
- It evokes a polar QUD about its prejacent

# The pragmatics of negation

(80) It's not raining

# The pragmatics of negation

(80) It's not raining

(81) QUD: Is it raining?

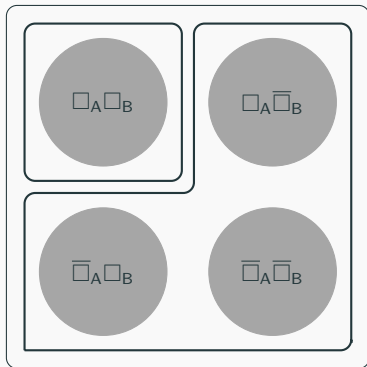
(82) It's not required that Mia buys pears and bananas.

## Putting it all together

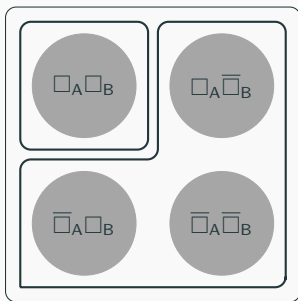
(82) It's not required that Mia buys pears and bananas.

(83) QUD: Is it required that Mia buys pears and bananas?

# Is it required that A and B?

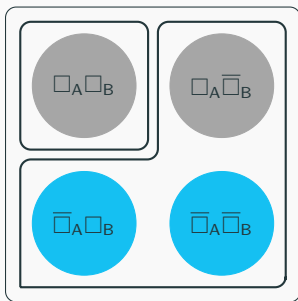


## Is it required that A and B?



{ It is not required that A  $\neg \square A$   
It is not required that B  $\neg \square B$  }

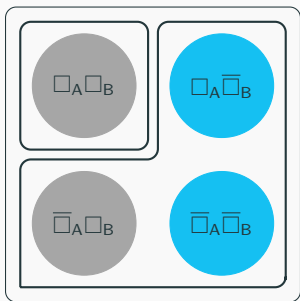
## Is it required that A and B?



$\left\{ \begin{array}{l} \text{It is not required that A} \quad \neg \Box A \\ \text{It is not required that B} \quad \neg \Box B \end{array} \right\}$



## Is it required that A and B?



$\left\{ \begin{array}{l} \text{It is not required that A} \quad \neg \Box A \\ \text{It is not required that B} \quad \neg \Box B \end{array} \right\}$

(84) EXH[ It is not required A and B] =  $\neg\Box A \vee \neg\Box B$   
*It is not required A or It is not required B*

(85) It's permitted that Mia buys pears or hamburgers.

---

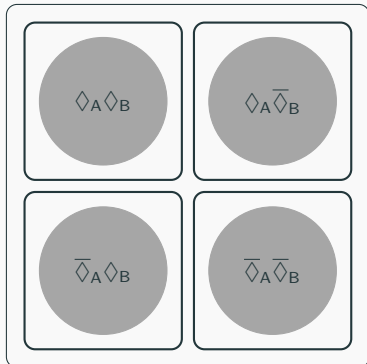
<sup>17</sup>Simons 2001, Romoli 2012, Marty and Romoli 2020

- (85) It's permitted that Mia buys pears or hamburgers.
- (86) QUD: What is Mia permitted to buy?

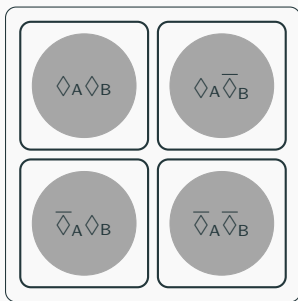
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<sup>17</sup>Simons 2001, Romoli 2012, Marty and Romoli 2020

## What is Mia permitted to buy?

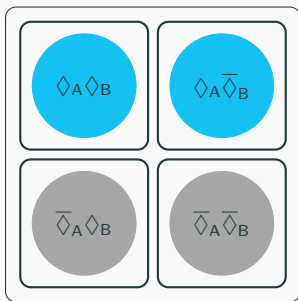


## What is Mia permitted to buy?



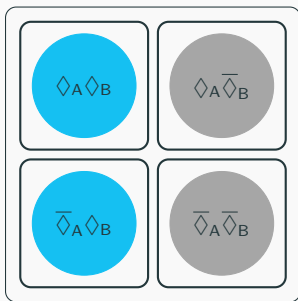
$\left\{ \begin{array}{l} \text{It is permitted that A } \diamond A \\ \text{It is permitted that B } \diamond B \end{array} \right\}$

## What is Mia permitted to buy?



$\left\{ \begin{array}{l} \text{It is permitted that A} \quad \Diamond A \\ \text{It is permitted that B} \quad \Diamond B \end{array} \right\}$

## What is Mia permitted to buy?



$\left\{ \begin{array}{l} \text{It is permitted that A} \quad \Diamond A \\ \text{It is permitted that B} \quad \Diamond B \end{array} \right\}$



$$(87) \quad \left\{ \begin{array}{l} \text{It is permitted that } A \quad \diamond A \\ \text{It is permitted that } B \quad \diamond B \end{array} \right\}$$

$$(88) \quad \text{EXH[ It is permitted } A \text{ or } B] = \\ \text{It is permitted } A \text{ and It is permitted } B$$

$$\diamond A \wedge \diamond B$$

(89) It's not required that Mia buys pears.

# The problem

- (89) It's not required that Mia buys pears.
- (90) QUD: Is it required that Mia buys pears?

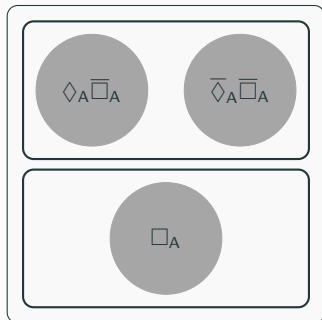


# The problem

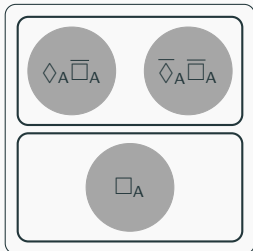
(91) EXH[ It is not required that A ] =  
It is not required that A but it is permitted that A ISI

(92)  $\left\{ \begin{array}{ll} \text{It is not required that A} & \neg\Box A \\ \text{It is not permitted that A} & \neg\Diamond A \end{array} \right\}$

# Is it required that A?

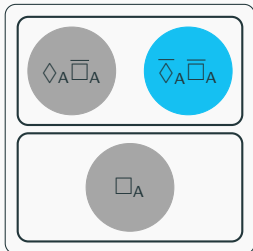


## Is it required that A?



{ It is not permitted that A  $\neg\Diamond A$  }

## Is it required that A?



{ It is not permitted that A  $\neg\Diamond A$  }



(93) EXH[ It is not required that A] =  
It is not required that A

NO ISI

- The idea allows to account for the difference between FC and NFC

- The idea allows to account for the difference between FC and NFC
- It incorrectly extends to predict that ISIs should be weaker than SIs

## Experiment 3

- Same as experiment 1 but we didn't use *both* and *either*

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- Same as experiment 1 but we didn't use *both* and *either*
- Results very similar, but higher rejection rate in NFC

# Experiment 4

- Motivation: understanding the difference between positive and negative free choice

## Experiment 4

- Motivation: understanding the difference between positive and negative free choice
- Comparing them to positive and negative ignorance implicatures

- (94) Mia bought avocados or berries.  
↪ *The speaker doesn't know which of the two she bought*

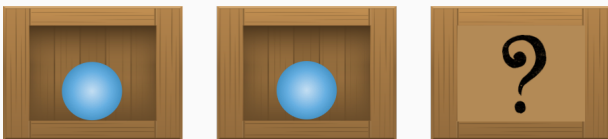


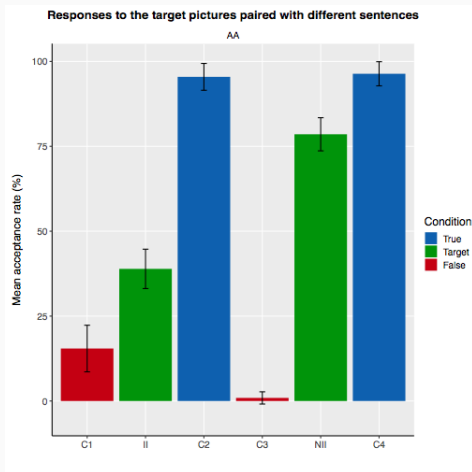
- (95) Mia didn't buy both avocados and berries.  
↪ *The speaker doesn't know which of the two she didn't buy*

- Mistery box task

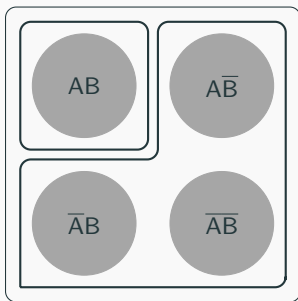
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<sup>18</sup>adapted from Noveck 2001; see also Moscati et al 2015



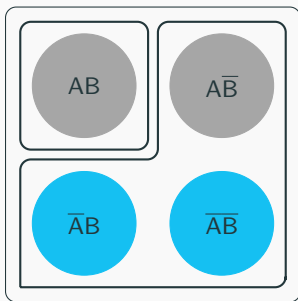


# Is it A and B?



$$\left\{ \begin{array}{ll} \text{not A} & \neg A \\ \text{not B} & \neg B \end{array} \right\}$$

## Is it required that A and B?



$$\left\{ \begin{array}{ll} \text{not } A & \neg A \\ \text{not } B & \neg B \end{array} \right\}$$

## No negative ignorance<sup>19</sup>

(96) It is not A and B

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<sup>19</sup>Provided a theory of ignorance based on alternatives e.g. not Fox 2007

## **The previous study**

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§ Semantics & Pragmatics Volume 2, Article 2: 1-33, 2009  
doi: 10.3765/sp.2.2

**Universal implicatures and free choice effects:  
experimental data\***

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*University College London*

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<sup>20</sup>Chemla 2009

# The previous study

- Comparing positive and negative free choice in French

# The previous study

- Comparing positive and negative free choice in French
- Using an inferential task

(97) John is allowed to give me the commentary or the dissertation.

- (97) John is allowed to give me the commentary or the dissertation.  
*John can choose which of the two he will give to the teacher*

## Comparing positive and negative free choice

(98) John does not have to give me the dissertation and the commentary.

- (98) John does not have to give me the dissertation and the commentary.  
*John can choose which of the two he will give to the teacher*

- Positive free choice received around 90% of endorsement rate



- Positive free choice received around 90% of endorsement rate
- Negative free choice was around 60%

# The problems

- No baseline for inference endorsement

# The problems

- **No baseline** for inference endorsement
- How do we know that it was really an inference?

# The problem<sup>21</sup>

- Particularly **problematic** given the inferential task

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<sup>21</sup>Geurts and Poscoulous 2009, Chemla and Spector 2011, Gotzner and Romoli 2018

# The problem<sup>21</sup>

- Particularly **problematic** given the inferential task
- **Inviting** endorsement of the candidate inference

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<sup>21</sup>Geurts and Poscoulous 2009, Chemla and Spector 2011, Gotzner and Romoli 2018

# The problem

The fact that the alleged inference was explicitly mentioned may have an effect on the derivation of the inference [...] even if it might **prevent us from drawing strong conclusions from absolute results**, the differences between conditions remains meaningful. (Chemla 2009; p. 14)

# The problems

- Also not using 'both' so not controlling for a potential role of the homogeneity of conjunction

- The results are **promising** and suggest that negative free choice is weaker than the positive one, if it is there



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- We also do not know what is the role of the homogeneity of '**and**'

- The results are **promising** and suggest that negative free choice is weaker than the positive one, if it is there
- But no baseline: we can't conclude that **negative free choice** is there
- We also do not know what is the role of the homogeneity of 'and'
- The debate is **not settled**